## **CHAPTER 7 PROJECT**

## A Meeting of Civilizations

A wandering wormhole picked up a community from each of the following civilizations and placed them in relatively close distance to each other on a new, habitable planet: Mayans, Babylonians, and Greeks. Once the Babylonians adjusted to their new surroundings, they set out exploring and discovered the Mayan civilization. After working through the communication difficulties of having different languages, the two communities decided to set up a trade system. However, since their numeration systems were so different, they first had to figure out how to translate values between the two systems.

- 1. First, we need to determine the basics of each numeration system. Determine the base number systems used by the Babylonians and the Mayans.
- 2. To initiate numerical conversions between the two civilizations, the Babylonians decided to create a table of the numerals from 1 through 59. Fill out the table (provided on the next page) of the first 59 values of the Mayan numeration system. (The Babylonian numeration system has been provided.)
- **3.** Describe how place value is represented in each numeration system. What kind of difficulties or confusions might arise from the differences in writing larger numbers between the systems.
- 4. Mathematical communication between the two civilizations holds some difficulty because each uses a different base number system and has different symbols for numerals. The Mayan system adds another layer of complexity by having a symbol for zero. How would you explain the use of the symbol zero to someone who is not familiar with the idea? What difficulties might arise from one system having a zero symbol and the other not having it? Would you, as a user of the Mayan system, try to convince the users of the Babylonian system to adopt the zero symbol or would you give up the zero symbol for communication purposes?
- 5. To convert numbers from the Babylonian system to the Mayan system (and vice versa), the two civilizations would not have converted the values first to base 10. This is because neither civilization used a base 10 system. Describe a method the two civilizations might use to convert numbers to and from each system. (Hint: Are there any patterns? Would a larger conversion table be necessary? Can you think of any other methods they might use?)
- **6.** After setting up a trade system with the Mayans, the Babylonians continued their exploration of their new world and discovered the Greek civilization. After working through the communication difficulties of having different languages, the two communities decided to set up a trade system. Determine the base number system used by the Greeks. Does the Greek system a positional system?
- 7. The Babylonians decided to add the Greek numerals to their table of Babylonian and Mayan numerals. Add the first 59 numerals of the Greek system to the table.
- **8.** Which of the two systems of most similar? Explain how the two systems are similar and explain how they are different.
- 9. To simplify trade, the three civilizations adopted a unified currency: gold coins. The Babylonians are the first to advertise a deal to both civilizations. They are willing to sell ≺ ≺ ∇∇∇∇ bales of hay for ∇∇∇ gold coins. Convert these values to both the Mayan and the Greek system.
- 10. The Greeks advertise that they are willing to sell bundles of wool to the other two civilizations. The wool comes in uniformly sized bundles. They are willing to sell  $\rho$  bundles of wool for  $\mu$   $\epsilon$  gold coins. Convert these values to both the Babylonian and the Mayan system.
- 11. The Mayans consider the offer from the Greeks and respond that they are only willing to pay gold coins for
  - bundles of wool. The Greeks counteroffer with  $G_{\epsilon}$  bundles of wool for  $\mu$  gold coins. The Mayans agree to the new deal as long as the Babylonians can also have the same deal. The Greeks accept. Translate the Mayan offer to Greek numerals and translate the Greek counteroffer into both Mayan numerals and Babylonian numbers.

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